# Dept of Mathematics and Statistics <br> King Fahd University of Petroleum \& Minerals 

AS450: Risk Modelling<br>Dr. Mohammad H. Omar<br>Major 1 Exam Term 231 FORM 001

Name $\qquad$ ID\#: $\qquad$ Serial \#:

## Instructions.

1. Mobile calculators, I-pad, smart watches, or communicable devices are disallowed.
a. Please do not bring your cell phones, smart watches, or other electronic devices in the exam.
b. If you bring these, switch them off and put them in the corner chair.
c. The phone must be switched off to avoid any disturbance during the exam
2. Any student caught with these devices switched on during the exam will be considered under the cheating rules of the University
3. If you finish the test earlier and want to leave the room, please do so quietly so not to disturb others taking the test.
a. No bathroom break during exam. You can only leave the room after the exam or use the bathroom before the exam starts.
b. No two person can leave the room at the same time.
c. No extra time will be provided for the time missed outside the classroom.
4. Only materials provided by the instructor can be present on the table during the exam.
5. While every attempt is made to avoid defective questions, sometimes they do occur. In the rare event that you believe a question is defective, the instructor cannot give you any guidance beyond these instructions.
6. Do not spend too much time on any one question. If a question seems too difficult, leave it and go on.
7. Use the blank portions of each page for your work. Extra blank pages can be provided if necessary.
a. If you use an extra page, indicate clearly your name and what problem you are working on.
8. Only problem-solving answers supported by work will be considered. Unsupported guesses will not be graded.
9. Use regular scientific calculators or SoA approved calculators only.
a. But write important steps to arrive at the solution of the problem-solving questions.
10. Record your final answers to the multiple-choice questions on the OMR sheet.
a. Submit the physical OMR page to your proctor
b. Submit your answers to problem-solving questions to your proctor

The test is 90 minutes, GOOD LUCK, and you may begin now!

Q1. Which of the following does not state the correct historical or current roles of investment banks?
A) original role of investment banks was to raise debt and equity funds for customers
B) original role of investment banks was to advise on corporate actions such as mergers and acquisitions
C) investment banks now buy and sell securities and derivatives
D) investment banks provide advise to clients how to manage mortgage accounts
E) investment banks monitors investment accounts for their customers

Q2. Which of the following correctly describes one of the two main sources of credit risk for an insurance company?
A) risk of reinsurer failure
B) risk due to failure of information technology
C) risk due to fraudulent claims
D) risk cashflows due to difference in foreign exchange from the intended currency
E) risk due to regulations and legislation from government

Q3. Which of the following is not part of the risk identification process?
A) The tools that can be used
B) the ways in which the tools are used
C) assessment of the nature of the risk
D) the way in which the risk is recorded
E) the assets involved in identifying the risks

Q4. Which of the following is true when using a SWOT analysis?
A) Weakness is not important when strength has been identified
B) Weakness is important only if it informs an organization of its exposure to a threat
C) SWOT analysis uncovers only positive prospects for future company's strategies
D) Increased regulation is one example of opportunities facing an organization
E) SWOT analysis should not be used for strategy development

Q5. Which of the following is not part of an Enterprise Risk Management framework?
A) assess the context in which the framework is operating
B) a consistent risk taxonomy is needed to promote an organization-wide understanding of risks
C) the risks to which an organization is exposed must be identified
D) implementing strategies to address risks
E) the CEO is solely responsible for the management of risks

Q6. Consider two insurance claims, $X$ and $Y$. The probability that claim $X$ is less than or equal to $\$ 40000$ is 0.85 , whilst the probability that claim $Y$ is less than or equal to $\$ 35000$ is 0.94 . If the claims are linked by a Gumbel copula with a parameter $\alpha$ of 2.5 , what is the probability that both $X$ is less than or equal to $\$ 40000$ and $Y$ is less than or equal to $\$ 35000$ ?
A) 0.1064
B) 0.6567
C) 0.8452
D) 0.8610
E) 0.8950

Q7. The probability that a particular project, $X$, will make a loss (that is, will produce a return of less than zero) is 0.15 , whilst the probability that another project, $Y$, will make a loss is 0.25 . The correlation measured using Kendall's tau, between returns on $X$ and $Y$ is 0.5 . Returns on $X$ and $Y$ are linked by a Clayton copula. Calculate the probability that both projects make a loss.
A) 0.1002
B) 0.1297
C) 0.2005
D) 0.2501
E) 0.5000

Q8. Compute the coefficient of lower tail dependence for a Gumbel copula with parameter $\alpha=4$.
A) -7
B) -3
C) 0
D) 5
E) 10

Q9. Consider the chief executives of firms $X$ and $Y$. Company specific shocks lead to firm $X$ replacing its chief executive on average once every 2 years, whilst company specific shocks lead to firm $Y$ replacing its chief executive on average once every 4 years. Furthermore, economywide shocks lead to firms replacing their chief executive once every 8 years. Assuming these shocks occur in line with Poisson distributions, what is the probability that the chief executive of firm $X$ stays in post for at least a further 3 years and that the chief executive of firm $Y$ stays in post for at least a further 4.5 years?
A) 0.04127
B) 0.04979
C) 0.15336
D) 0.18498
E) 0.0334

Your instructor's name: Dr. Mohammad H. Omar Name: $\qquad$ ID \#: $\qquad$ Serial\#: $\qquad$
Part 1 (2 marks each). Please mark the correct answer to each of the questions by completely darkening the oval of your choice with a dark pen or pencil.

| MULTIPLE <br> CHOICE: | A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Q1 | O | O | O | O | O |
| Q2 | O | O | O | O | O |
| Q3 | O | O | O | O | O |
| Q4 | O | O | O | O | O |
| Q5 | O | O | O | O | O |


| MULTIPLE <br> CHOICE: | A | B | C | D | E |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Q6 | 0 | 0 | 0 | 0 | 0 |
| Q7 | 0 | 0 | 0 | 0 | 0 |
| Q8 | 0 | 0 | 0 | 0 | 0 |
| Q9 | 0 | 0 | 0 | 0 | 0 |
|  |  |  |  |  |  |



Code: 001

Q10. (2+2=4 marks) Consider claims on two insurance products, $X$ and $Y$. An actuarial analyst is using the Frechet-Hoeffding's copula with $p=0.3$ and $q=0.9$ to model the joint probabilities of claims from these two insurance products. Calculate the following concordance index between $X$ and $Y$ :
a) the Kendall's Tau
b) the Spearman rho


Q11. ( $\mathbf{1 + 3}=\mathbf{4}$ marks) Some $R$ output on a multivariate analysis of the Fisher's iris data is given below

| Skewness Kurtosis |  | Beta-hat kappa p-val <br> 10.22740 81.819229 $1.923968 \mathrm{e}-09$ <br> 32.23929 4.119643 $3.794604 \mathrm{e}-05$ | kappa $p-v a 1$ <br> 81.819229 $1.923968 \mathrm{e}-09$ <br> 4.119643 $3.794604 \mathrm{e}-05$ |  |  |  | 33 | 5980 | 1426.76 | 0.197653 | 950 | 2.7677 | 0.59741 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 34 |  |  |  |  | 5318 | 990.388 | 0.326635 | 950 | 2.2119 | 0.69685 |
|  |  | 35 |  |  |  |  | 7392 | 1350.76 | 0.154192 | 950 | 6.9421 | 0.13898 |
| area |  |  | $\begin{aligned} & \text { peri } \\ & 2791.9 \end{aligned}$ | shape | perm | mahal | P | $\begin{aligned} & 36 \\ & 37 \end{aligned}$ | $\begin{aligned} & 7894 \\ & 3469 \end{aligned}$ | $\begin{aligned} & 1461.06 \\ & 1376.7 \end{aligned}$ | $\begin{aligned} & 0.276016 \\ & 0.176969 \end{aligned}$ | 950 | $3.6577$ | 0.45431 |
|  |  | 100 |  |  |  |  |  |  |  |  |  | 5.1507 | 0.27218 |
| 1 | 4990 |  |  | 0.0903296 | 6.3 | 3.9200 | 0.41694 | 38 | 1468 | 476.322 | 0.438712 | 100 | 22.8964 | $0.00013$ |
| 2 | 7002 | 3892.6 | 0.148622 | 6.3 | 2.6587 | 0.61646 | 39 | 3524 | 1189.46 | 0.163586 | 100 | 6.3458 | 0.17477 |
| 3 | 7558 | 3930.66 | 0.183312 | 6.3 | 1.9069 | 0.75288 | 40 | 5267 |  | 0.253832 | 100 | 5.5521 | 0.23519 |
| 4 | 7352 | 3869.32 | 0.117063 | 6.3 | 2.3503 | 0.67163 | 41 | 5048 | 941.543 | 0.328641 | 1300 | 4.8364 | 0.30450 |
| 5 | 7943 | 3948.54 | 0.122417 | 17.1 | 1.8301 | 0.76696 | 42 | 1016 | 308.642 | 0.230081 | 1300 | 12.2679 | 0.01547 |
| 6 | 7979 | 4010.15 | 0.167045 | 17.1 | 1.5584 | 0.81625 | 43 | 5605 | 1145.69 | 0.464125 | 1300 | 10.3082 | 0.03554 |
| 7 | 9333 | 4345.75 | 0.189651 | 17.1 | 1.5106 | 0.82476 | 44 | 8793 | $2280.49$ | 0.420477 | $1300$ | 10.0765 | 0.039160.70946 |
| 8 | 8209 | 4344.75 | 0.164127 | 17.1 | 2.7005 | 0.60912 |  |  |  |  | $\begin{aligned} & 580 \\ & 580 \\ & 580 \\ & 580 \\ & \hline \end{aligned}$ | $\begin{aligned} & 2.1431 \\ & 4.7576 \\ & 1.8320 \\ & 15.6163 \end{aligned}$ |  |
| 9 | 8393 | 3682.04 | 0.203654 | 119 | 0.6335 | 0.95927 | $\begin{aligned} & 46 \\ & 47 \\ & 48 \end{aligned}$ | $\begin{aligned} & 3475 \\ & 1651 \\ & 5514 \\ & 9718 \\ & \hline \end{aligned}$ | $\begin{aligned} & 1174.11 \\ & 597.808 \\ & 1455.88 \\ & 1485.58 \\ & \hline \end{aligned}$ | $\begin{aligned} & 0.200744 \\ & 0.262651 \\ & 0.182453 \\ & 0.200447 \\ & \hline \end{aligned}$ |  |  | $\begin{aligned} & 0.70946 \\ & 0.31309 \\ & 0.76662 \\ & 0.00358 \end{aligned}$ |
| 10 | 6425 | 3098.65 | 0.162394 | 119 | 1.0451 | 0.90288 |  |  |  |  |  |  |  |
| 11 | 9364 | 4480.05 | 0.150944 | 119 | 2.3524 | 0.67125 |  |  |  |  |  |  |  |
| 12 | 8624 | 3986.24 | 0.148141 | 119 | 1.2454 | 0.87056 |  |  |  |  |  |  |  |
| 13 | 10651 | 4036.54 | 0.228595 | 82.4 | 2.4566 | 0.65243 |  |  |  |  |  |  |  |
| 14 | 8868 | 3518.04 | 0.231623 | 82.4 | 1.3505 | 0.85275 |  |  |  |  |  |  |  |
| 15 | 9417 | 3999.37 | 0.172567 | 82.4 | 0.9438 | 0.91819 |  |  |  |  |  |  |  |
| 16 | 8874 | 3629.07 | 0.153481 | 82.4 | 1.0426 | 0.90326 |  |  |  | Q plo | or |  |  |
| 17 | 10962 | 4608.66 | 0.204314 | 58.6 | 2.1918 | 0.70054 |  |  |  |  |  |  |  |
| 18 | 10743 | 4787.62 | 0.262727 | 58.6 | 3.9161 | 0.41748 |  |  |  |  |  |  |  |
| 19 | 11878 | 4864.22 | 0.200071 | 58.6 | 3.1275 | 0.53673 |  |  |  |  |  |  |  |
| 20 | 9867 | 4479.41 | 0.14481 | 58.6 | 1.8387 | 0.76540 |  |  |  |  |  | $\bigcirc$ |  |
| 21 | 7838 | 3428.74 | 0.113852 | 142 | 1.5689 | 0.81438 |  | $\stackrel{\square}{\square}$ |  |  |  |  |  |
| 22 | 11876 | 4353.14 | 0.291029 | 142 | 5.1993 | 0.26745 |  |  |  |  |  |  |  |
| 23 | 12212 | 4697.65 | 0.240077 | 142 | 3.9513 | 0.41264 |  |  |  |  |  |  |  |
| 24 | 8233 | 3518.44 | 0.161865 | 142 | 0.5756 | 0.96574 |  |  |  |  |  |  |  |
| 25 | 6360 | 1977.39 | 0.280887 | 740 | 0.7816 | 0.94090 |  |  | 2 | 46 | 8 |  |  |
| 26 | 4193 | 1379.35 | 0.179455 | 740 | 2.4518 | 0.65329 |  |  |  |  |  |  |  |
| 27 | 7416 | 1916.24 | 0.191802 | 740 | 2.1678 | 0.70493 |  |  |  | (ppoi | 48) | $=4$ |  |
| 28 | 5246 | 1585.42 | 0.133083 | 740 | 3.6781 | 0.45132 |  |  |  | 号 | (48) | - 4) |  |
| 29 | 6509 | 1851.21 | 0.225214 | 890 | 1.6606 | 0.79787 |  |  |  |  |  |  |  |
| 30 | 4895 | 1239.66 | 0.341273 | 890 | 2.6627 | 0.61576 |  |  |  |  |  |  |  |
| 31 | 6775 | 1728.14 | 0.311646 | 890 | 1.6348 | 0.80252 |  |  |  | QQ p |  |  |  |
| 32 | 7894 | 1461.06 | 0.276016 | 890 | 3.7257 | 0.44440 |  |  |  |  |  |  |  |
|  |  | Provide | the estin | te of | the m | tivaria |  | SS-t | para | ter. |  |  |  |
|  |  | Provide given | the corr bove. | t dec | ision | teria a |  | usion | n the | a based | the | alysis |  |

