

**King Fahd University of Petroleum and Minerals**  
**Department of Mathematics**  
**SYLLABUS**  
Semester I, 2022-2023 (231)

(Instructor: Dr. Adel Khalfallah  
[khelifa@kfupm.edu.sa](mailto:khelifa@kfupm.edu.sa)  
Office B#5 201-5)

**Course #:** Math 533  
**Title:** Complex Variables  
**Textbook:** Complex Analysis, Ahlfors (3<sup>rd</sup> Edition)

**Course description:** Analytic functions. Cauchy's theorem and consequences. Singularities and expansion theorems. Maximum modulus principle. Residue theorem and its application. Compactness and convergence in spaces of analytic functions. Weierstrass and Mittag-Leffler representation theorems. Elementary conformal mappings.

**Objectives:**

1. Demonstrate accurate and efficient use of complex analysis techniques.
2. Demonstrate capacity for mathematical reasoning through analyzing, proving and explaining concepts from complex analysis.

Wk	Chapters	Material
1	Chapter 1,2	The Algebra of Complex Numbers. Concept of Analytic Functions: Limits – Continuity – Analyticity.
2	Chapter 2	The Cauchy-Riemann Equations, Harmonic functions
3		The Exponential, Trigonometric and Logarithmic Functions.
4	Chapter 4	Fundamental Theorems

5		Cauchy's Integral Formula
6		Local Properties of Analytical Functions
7		General Form of Cauchy's Theorem
8		Calculus of Residues
9		Harmonic Functions
10	Chapter 5	Power Series Expansions
11		Partial Fraction and Factorization
12-13	Chapter 6	Conformal Mapping. Dirichlet's Problem
14-15	Presentations	

**Evaluation Policy:**

Major Exam I: 25 %

Major Exam II: 25 %

Final Exam : 35 %

Presentation 5%

Assignments: 10%

**References**

- 1) Conway, *Functions of One Complex Variable*, 2nd ed., Springer-Verlag, 1978
- 2) Ponnusamy and Silvermann, *Complex Variables with applications*, Birkhauser 2006
- 3) R.E. Greene, S.G. Krantz, *Function Theory of One Complex Variable*, AMS, 2001.
- 4) Elias M. Stein and R. Shakarchi, *Complex Analysis*, Princeton University Press, 2003