King Fahd University of Petroleum & Minerals Department of Mathematics

Syllabus of the Comprehensive Exam MATH 581 Advanced Linear Programming

Topics

- **Theory of linear programming**: Simplex Algorithm, Two phase simplex method, Big-M simplex method.
- **Duality theory**: weak and strong duality theorems, Complementary slackness conditions, Dual simplex method.
- Integer Programming: Branch and Bound, and Cutting Plane methods.
- Transportation problem: North-West corner, Least cost and Vogel's methods, and u-v-method for optimality) and assignment problem (Hungarian method.
- Linear fractional programming: Charnes-Cooper method.
- Convex functions and properties: Karush-Kuhn Tucker conditions, Wolfe method.
- Sensitivity Analysis: Change in cost vector, Change in right-hand side, Change in adding new constraints, Adding new decision variables, and change in the coefficient of a matrix A.
- Revised Simplex Method: Revised two-phase Simplex Method, Revised Big-M Simplex Method.
- Karmarkar's Algorithm for linear programming problems

References

- Robert J. Vanderbei, *Linear Programming Foundations and Extensions*, 5th Edition Springer (2020)
- Hamdy A. Taha, Operations Research An Introduction, 10th Edition, 2017, Pearson