

**King Fahd University of Petroleum and Minerals**  
**Department of Mathematics & Statistics**  
**Syllabus MATH 645**  
**AY: 2023-2024 (T231)**  
**Dr. Othman Echi**  
**Office : 319-Building 5**

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**Title:** Combinatorics & Graph Theory

**Textbook:** Applied combinatorics (6th ed), Alan Tucker, Wiley, 2012.

**Description:** Enumerative analysis, generating functions. Sorting and searching. Theory of codes. Block design. Computational combinatorics. Methods of transforming combinatorial ideas into efficient algorithms. Algorithms on graphs, network flow.

**Office Hours:** Every Monday from 10:00 to 11:00 AM

**Grading Policy:**

| Exam 1 | Exam 2 | Exam 3 | HW | Presentations | Final Exam |
|--------|--------|--------|----|---------------|------------|
| 20%    | 20%    | 20%    | 5% | 5%            | 30%        |
| tba    | tba    | tba    |    |               | tba        |

| Week   | Topics   |
|--------|--|
| 1, 2   | <b>Elements of Graph Theory:</b> Graphs, Isomorphisms, Hamiltonian Graphs, Fleury's algorithm, planar graphs, subdivision, minor, dual of a graph, maximal planar graphs, Euler's formula, ... |
| 3,4    | <b>Covering circuits and Graph colouring:</b> Eulerian and semi-Eulerian graphs, colouring, colouring theorems.  |
| 5, 6   | <b>Trees:</b> Properties of trees, shortest paths, the traveling Salesperson Problem, minimum spanning trees   |
| 7,8    | <b>General Counting Methods for arrangements and selections:</b> Counting principles, Binomial Identities, multinomial coefficients, ...   |
| 9      | <b>Generating Functions:</b> Calculating coefficients of generating functions, exponential generating functions  |
| 10     | <b>Recurrence Relations:</b> Recurrence relations models, linear recurrence relations, recurrence relations and generating functions.  |
| 11     | <b>Mobius Inversion Formula in Posets:</b> Incidence algebra of a poset, Mobius inversion formula, Exclusion-inclusion.  |
| 12, 13 | <b>Polya's Enumeration Formulas:</b> Group action, Burnside's Formula, Polya's formula.  |
| 14, 15 | <b>Introduction to Combinatorics on Words:</b> Primitive words, languages, counting special kinds of words, codes, ...   |