

1. If $y = (1 + e^x)^{\ln x}$, then $y'(1) =$

- (a) $\ln(1 + e)$ _____ (correct)
(b) 0
(c) 1
(d) e
(e) $(1 + e)$

2. The slope of the tangent line to $y = (x + 1)(x + 2)^2(x + 3)^2$ at $x = 0$ is equal to

- (a) 96 _____ (correct)
(b) 84
(c) 64
(d) 50
(e) 20

3. If $x^2 + 3x + y^2 = 4y$, then $\frac{d^2y}{dx^2}$ when $x = 0$ and $y = 0$ is equal to

- (a) $\frac{25}{32}$ _____ (correct)
- (b) $\frac{9}{32}$
- (c) $-\frac{25}{32}$
- (d) $\frac{16}{32}$
- (e) $\frac{-9}{32}$

4. At $x = -2$ the function $f(x) = x^2e^x$ has

- (a) a relative maximum _____ (correct)
- (b) a relative minimum
- (c) an absolute maximum
- (d) an absolute minimum
- (e) neither maximum nor minimum

5. The absolute maximum of $f(x) = \frac{x}{x^2 + 1}$ over the interval $[0, 2]$ is equal to

- (a) $\frac{1}{2}$ _____(correct)
- (b) 1
- (c) $\frac{2}{5}$
- (d) $\frac{1}{5}$
- (e) 2

6. The function $f(x) = x^{2/3}$ over the interval $[-8, 8]$ has the

- (a) absolute maximum at $x = 8$ and $x = -8$ _____(correct)
- (b) absolute minimum at $x = 8$
- (c) absolute maximum at $x = 0$
- (d) absolute minimum at $x = -8$ only
- (e) absolute maximum at $x = -8$ only

7. The function $f(x) = \frac{1}{10}x^5 - 3x^3 + 17x + 43$ is concave up on the interval

- (a) $(-3, 0) \cup (3, \infty)$ _____(correct)
(b) $(-\infty, 0) \cup (3, \infty)$
(c) $(-3, 3)$
(d) $(-3, \infty)$
(e) $(-\infty, -3) \cup (0, 3)$

8. The number of inflection points of the function $f(x) = \frac{x^2 + 1}{x^2 - 2}$ is equal to

- (a) 0 _____(correct)
(b) 1
(c) 2
(d) 3
(e) 4

9. At $x = -\frac{7}{2}$ the function $y = (x^2 + 7x + 10)^2$ has

- (a) a relative maximum _____(correct)
- (b) a relative minimum
- (c) an absolute maximum
- (d) an absolute minimum
- (e) an inflection point

10. At $x = 0.25$ the function $y = -4x^2 + 2x - 8$ has

- (a) an absolute maximum _____(correct)
- (b) a relative minimum
- (c) a relative maximum
- (d) an absolute minimum
- (e) an inflection point

11. The function $f(x) = 13e^{-x}$ has

- (a) one horizontal asymptote _____(correct)
- (b) one vertical asymptote
- (c) one vertical and one horizontal asymptote
- (d) no asymptotes
- (e) one horizontal and one oblique asymptote

12. The slope of the oblique asymptote of

$$f(x) = \frac{8x^2 + 9x + 5}{4x - 7}$$

is equal to

- (a) 2 _____(correct)
- (b) $\frac{8}{7}$
- (c) -2
- (d) 8
- (e) $\frac{-8}{7}$

13. For a monopolist's product, the demand function $p = 85 - 0.05q$ and the cost function is $c = 600 + 35q$. The maximum profit occurs at the price of

- (a) \$60 _____(correct)
- (b) \$600
- (c) \$500
- (d) \$20
- (e) \$100

14. The maximum volume of an open-top box with a square base constructed from 192 ft^2 of material is equal to

- (a) 256 ft^3 _____(correct)
- (b) 200 ft^3
- (c) 400 ft^3
- (d) 8 ft^3
- (e) 10 ft^3

15. Let $f(x) = x^{3x}$, then by using the differentials $f(0.98) \approx$

- (a) 0.94 _____ (correct)
(b) 0.98
(c) 0.90
(d) 0.02
(e) -0.02

16.

$$\int (6e^u - u^3(\sqrt{u} + 1)) du =$$

- (a) $6e^u - \frac{2}{9}u^{\frac{9}{2}} - \frac{u^4}{4} + C$ _____ (correct)
(b) $6e^u - \frac{12}{9}u^{\frac{9}{2}} - \frac{3u^4}{2} + C$
(c) $6e^u - \frac{2}{9}u^{\frac{9}{2}} + \frac{u^4}{4} + C$
(d) $6ue^u - \frac{2}{9}u^{\frac{9}{2}} + \frac{u^4}{4} + C$
(e) $6e^u - \frac{9}{2}u^{\frac{9}{2}} - 4u^4 + C$

17.

$$\int \frac{x^4 - 5x^2 + 2x}{5x^2} dx =$$

- (a) $\frac{x^3}{15} - x + \frac{2}{5} \ln|x| + C$ _____(correct)
- (b) $\frac{x^3}{3} + \frac{2}{5} \ln|x| + C$
- (c) $\frac{x^3}{15} - 5x + 2 \ln|x| + C$
- (d) $\frac{x^3}{15} - 5x + \frac{2}{3} \ln|x| + C$
- (e) $2x^2 - x + \frac{2}{5} \ln|x + 1| + C$

18. The marginal revenue of a product is

$$\frac{dr}{dq} = 2000 - 20q - 3q^2.$$

Then the unit price when producing 30 units $p(30) =$

- (a) 800 _____(correct)
- (b) 1600
- (c) 2000
- (d) 500
- (e) 1800

19. If $y' = \frac{5}{\sqrt{x}}$ and $y(9) = 50$, then $y(16) =$

- (a) 60 _____(correct)
(b) 80
(c) 90
(d) $\frac{1}{4}$
(e) 4

20.

$$\int x\sqrt{(8-5x^2)^3} dx =$$

- (a) $-\frac{1}{25}(8-5x^2)^{\frac{5}{2}} + C$ _____(correct)
(b) $-\frac{1}{50}(8-5x^2)^{\frac{5}{2}} + C$
(c) $\frac{1}{25}(8-5x^2)^{\frac{1}{2}} + C$
(d) $\frac{1}{25}(8-5x^2)^{\frac{5}{2}} + C$
(e) $-\frac{1}{10}(8-5x^2)^{\frac{3}{2}} + C$