## King Fahd University of Petroleum and Minerals **Department of Mathematics and Statistics SYLLABUS** Semester II, 2022-2023 (222) (Dr. Abdeslam MIMOUNI)

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Course #: Math 323 (Formerly named Math 345)

Title: Modern Algebra I

Prerequisite: MATH 210 or (ICS 253, ICS 254)

Textbook:

Contemporary Abstract Algebra by J. A. Gallian, eighth edition (2013)

**Objectives:** This course is intended to introduce students to fundamental concepts and techniques in abstract algebra and to provide students with appropriate background for more advanced courses in mathematics.

Week #	Date	Chapter	Topics
1	Jan. 15-19	2	Groups, Definitions, Examples, Elementary Properties
		3	Finite Groups, Subgroups: Terminology and notation, Subgroup Tests
2	Jan. 22-26	3	Examples of Subgroups
		4	Cyclic groups : Properties of Cyclic Groups
3	Jan. 29-	4	Classification of Subgroups of Cyclic Groups
	Feb. 02	5	Permutation groups: Notation&Definition, Cycle notation
4	Feb.05-09	5	Properties of Permutations
		6	Isomorphisms: Examples & Definition, Cayley's Theorem
5	Feb. 12-16	6	Properties of Isomorphisms, Automorphisms
		7	Cosets and Lagrange's theorem: Properties of Cosets, Lagrange's
			Theorem & Consequences
6	Feb. 19-21	8	External Direct Product: Definition, Examples, Properties of Ex. Dir.
		9	Prod.
			Normal subgroups and Factor groups: Normal Subgroups, Factor groups
7	Feb.26-	9	Internal Direct Products
	Mar. 02	10	Group Homomorphisms: Definition, Examples, Properties
			Saudi Foundation Day 22-23 February
8	Mar. 05-09	10	The First Isomorphism Theorem
		11	Fundamental Theorem of Finite Abelian Groups: The Fundamental
			Theorem, The Isomorphism Classes of Abelian Groups
9	Mar. 12-16	12	Introduction to rings: Definition, Examples, Properties of Rings,
10			Subrings
10	Mar. 19-23	13	Integral Domains: Definition, Examples, Fields, Characteristic of a Ring.
11	Mar. 26-30	14	Ideals and Factor Rings: Ideals, Factor Rings, Prime and Maximal Ideals.
12	Apr. 02-06	15	Ring Homomorphism: Definition, Examples, Properties of Ring
			Homomorphisms, The Field of Quotients
13	Apr. 09-13	16	Polynomial Rings: Notation and Terminology, The Division Algorithm
			and Consequences.
			Eid Al-Fitr Holidays 14-27 April
14	Apr. 30-	17	Factorization of Polynomials: Reducibility Tests, Irreducibility Tests,
	May 04		Unique Factorization in Z[x]
15	May 7-11	18	Divisibility in Integral Domains: Irreducibles, Primes, Unique
			Factorization Domains.
	May 14-15	Catch-up	Normal Wednesday and Thursday classes

(\*) No Makeup is given under any circumstance. If a student misses an assessment for a legitimate reason (e.g., medical emergency), his final grade will be determined based on the non-missed assessments.

Learning Outcomes: Upon completion of this course, students should be able to

- Define normal subgroups, factor groups, homomorphisms
- Discuss the fundamental theorem of finite Abelian groups
- Explain integral domains and fields
- Define ideals, factor rings and ring homomorphisms

• Explain factorization of polynomials over a field, factor rings of polynomials over a field

• Define irreducible elements and unique factorization

• Discuss principal ideal domains

Academic Integrity: All KFUPM ethic policies apply in this course. University Policy on Attendance: A DN grade will be awarded to any student who accumulates 9 absences Office Hours and Contact Information: Office hours: UTR 9:00 a.m. – 10:00 a.m.

## **Homework**

Chapter 2	Exercises: 22-34-52
Chapter 3	Exercises: 4-12-32
Chapter 4	Exercises: 14-20-42
Chapter 5	Exercises: 22-26-38
Chapter 6	Exercises: 2-10-42
Chapter 7	Exercises: 6-12-48
Chapter 8	Exercises: 6-22-38
Chapter 9	Exercises: 10-38-48
Chapter 10	Exercises: 6-14-20
Chapter 11	Exercises: 2-8-22
Chapter 12	Exercises: 4-8-12
Chapter 13	Exercises: 14-30-46
Chapter 14	Exercises: 14-16-26
Chapter 15	Exercises: 12-24-52
Chapter 16	Exercises: 4-10-20
Chapter 17	Exercises: 10-20-30
Chapter 18	Exercises: 4-12-28

## **Grading Policy.**

Homework: **Out of: 40.** Major Exam 1: February 20, 2023, Chapters 2-6. Out of: 80. Major Exam 2: March 13, 2023, Chapters 7-11. **Out of: 80.** Final Exam: Announced by the Registrar. **Out of: 100. Total: Out of: 300.** 

A+: 270 (90% or more), F: <150 (50%)