King Fahd University of Petroleum and Minerals Department of Mathematics MATH-562: Fundamentals of Option Pricing Term 212

Instructor: Dr. Brahim Mezerdi **Phone Office**: 013 – 860 4197 **Office Hours**: 2:00 pm – 3:00 pm UT Office: 5 - 330 E-mail: <u>brahim.mezerdi@kfupm.edu.sa</u> Class: 5:20 pm - 6:35 pm U.T Location: Blg # 59 - 1009

(3-0-3)

Course Objectives:

Introduce discrete and continuous time finance and the theory and practice of derivative pricing and hedging. Provide students with the mathematical skills needed for the valuation of derivatives. Focus will be on the application of results rather than their mathematical derivation. Be able to apply of stochastic methods to analyse and solve the famous Black-Scholes formula, to price options.

Course Description:

MATH562: Fundamentals of Option Pricing

Basic principles of option pricing, binomial model, the Black-Scholes model, arbitrage, complete and incomplete markets, trading strategies, European options, American options. Topics include Risk-neutral Valuation, options on stock Indices, currencies, futures, the Greek letters, Interest Rate Derivatives, Black-Scholes PDE and formula.

Pre-requisite: MATH 564

Textbook: Hugo D. Junghenn, An Introduction to Financial Mathematics, Option Valuation. Chapman and Hall/CRC, Second Edition 2019.

Reference: Robert L. McDonald (2009), Derivative Markets. Pearson, Third Edition, 2013.

Assessment*

Activity	Weight
Class Evaluation (quizzes)	10%
Homework	20%
Midterm Exam	30%
Final Exam (Comprehensive)	40%

Grade Assignment

Relative Grading based on overall performance of the students registered in this course.

Academic Integrity

All KFUPM policies regarding ethics and academic honesty apply to this course.

General Notes

Students are encouraged to regularly check the blackboard announcements.

Syllabus (Tentative)

Week	Sections	Topics
1		Basic finance
	1.1 - 1.5	Interest rate, Inflation, Annuities
		• Bonds, Internal rate of return
2		Probability Spaces
2	2.1 - 2.2	Sample spaces and events
		 Discrete probability spaces
3		Probability Spaces
-	2.4 - 2.5	Conditional probability
	_	• independence
4	33-34	Random Variables
	515 511	Discrete random variables
		Continuous random variables
5	26.20	Random Variables
	3.0-3.8	Independent random variables
		Identically random variables
		Sums independent random variables
6	4.1 – 4.3	Options and arbitrage
		• The price of an asset
		 Alonage Classification of derivatives
7		Options and arbitrage
	4.4 – 4.9	• Forwards and currency forwards
		• Futurs
		Call and Put Options
		Properties of options
8	5.1 - 5.2	Discrete time portfolio processes
		Discrete time stochastic processes
		Portfolios processes and the value process
9	5.3 - 5.5	Discrete time portfolio processes
		 Self financing trading strategies Equivalent abaracterizations of self financing
		 Option valuation by portfolios
10		Expectation and variance
	6.6 - 6.7	• The strong law of large numbers
		• The central limit theorem
11	71 72	The Binomial Model
	/.1 - /.2	Construction of the binomial model
		• Completeness and arbitrage in the
		binomial model
	11.1 - 11.2	Stochastic calculus
12	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Continuous time stochastic processes
		Brownian motion and geometric Brownain motion
	11.3 – 11.5	Stochastic calculus
13		Stochastic integrals
		Ito formula
		Stochastic differential equations
	12.1 - 12.3	Black Scholes Merton Model
14		• The stock price SDE
		Continuous time portfolios
		The Black Scholes formula
	Eid Al-	Fitr Holidays April 24-May 7

15	12.4	 Black Scholes Merton Model Properties of the Black Scholes call function
16		Review and catch up